



$$3^h + 2^h \rightarrow 2.44^h$$

$$O(2^n k^2)$$

$$O(2.0001^n)$$

for $m = 1..2^h - 1$:

dp[m] = +∞

for ($s = m; s \neq 0; s = (s-1) \& m$)

if ok[s]:

dp[m] = dp[m & s] + 1

for (m)
for (SSm)



$$2^{|m|}$$

$$\sum_{k=0}^n 2^k \binom{n}{k} = 3^n$$

$$\sum_{k=0}^n 2 \cdot 4^k \binom{n}{k} =$$

$$2 \cdot 4^n$$



```

def List(Cur, Rem) {
  if (Rem == 0)
    print(Cur)
  return

```



$\forall v \in \text{Rem}, \text{deg}_{\text{Rem}}[v] \geq \text{min}$ (n)

① List(Cur ∪ {v}, Rem \ {v}) ∩ G[v]

② for $u \in (G[v] \cap \text{Rem})$:
 List(Cur ∪ {u}, Rem \ {u}) ∩ G[u]





$$T(n) \leftarrow (k+1) T(n-(k+1))$$

$$k = \text{deg}(u)$$

$$T(n) = \max_{k'} k' T(n-k')$$

$$T(n) = \Theta(\lambda^n)$$

$$\lambda^n = k' \lambda^{n-k'}$$

$$\lambda^{k'} = k'$$

$$\lambda = (k')^{1/k'}$$

$$\max_{k'} (k')^{1/k'}$$

$$(x^{1/x})'$$

 $x=e$

$$k'=1 \Rightarrow 1$$

$$k'=2 \Rightarrow 2^{1/2} = 1.4142 \dots \approx e$$

$$k'=3 \Rightarrow 3^{1/3} = 1.4422$$

$$k'=4 \Rightarrow 4^{1/4} = 1.4142$$

$$k'=5 \Rightarrow 5^{1/5} = 1.37$$

2.4423

Meet In The Middle

Subset Sum

$x_1 \dots x_n$

3 на половина сумами S? nS
 2^n

$$n = 42$$

$$S = 10^8$$

$$2^{n/2}$$

$$dp[i][S] = 1/0$$

$1 \rightarrow i, S \Rightarrow$ можно или
нельзя?

$$dp[i][S] = dp[i-1][S] \\ \text{or } dp[i-1][S-x_i]$$



$n/2$ $n/2$
 $2^{n/2}$ $2^{n/2}$
 L R



for call: 1) Key Min. $O(2^{n/2})$
 if $S = L \cup R$: 2) $\text{Cost}(L, R) + O(5/24n)$
 print(Yes) $O(2^{n/2}n)$

Пример с стоимостями:

x_1, \dots, x_n

y_1, \dots, y_n

$$x_{i_1} + \dots + x_{i_k} \leq S$$

$$y_{i_1} + \dots + y_{i_k} \rightarrow \text{Max}$$

$$O(nS)$$

$$2^n$$

$$2^{n/2}$$



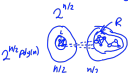
for $(x_{sum}, y_{sum}) \in L$:
 when $(x', y') \in R$: $x' \in S - x_{sum}$
 $y' \in \text{max}$

$$2^{h/2} - h$$

Klique



$2^{n/2}$ poly(n)



$\text{MAXCLIQUE}[R] - 1$
 $|R|, R\text{-klique}$
 $\text{MAX}(\text{MAXCLIQUE}[R-1],$
 VAR

$2^{n/2}$ poly(n)

$f(n) = \text{MAXCLIQUE}[G]$
 VEMSK

3
 $2^{n/2}$ poly(n)

$$|L| + \text{MAXCLIQUE}(P[L])$$



$$2^h$$

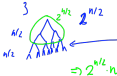


$$2^h$$

$\text{findClique}(\text{Set})$ { if/cache } return
 if (Set == 0) return 0;



$V \leftarrow \text{min}$ homogeneity among set
 return $\text{MAX}(\text{findClique}(\text{Set} \setminus \{V\}),$
 $\text{Cache}[\text{set}]) + \text{findClique}(\text{Set} \cap \{V\})$



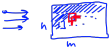
DP по узлам решетки
(классический)



гиперплоск.



пересор.



$\text{Grid}(l)$

$$2 \cdot \frac{h \ln / 2}{h} \cdot h \ln$$

$$\downarrow$$

$$2^m$$

Crute (State) if state in cache:
return cache[state]
if full:
return 1

return cache.put(state, crute(state)) +
crute(state + 1)

010
011
010



2^m poly(n)

call calc(n-1)



Num 2^m
 $dp[calc][mask]$
 $0 \dots 2^m - 1$